

Algebraic Proof (H)

A collection of 9-1 Maths GCSE Sample and Specimen questions from AQA, OCR, Pearson-Edexcel and WJEC Eduqas.

Name:	Rebecca Simkins
Total Marks:	

1. Prove algebraically that

 $(2n + 1)^{2} - (2n + 1) \text{ is an even number}$ for all positive integer values of n. $4n^{2} + 4n + 1 - 2n - 1$ $= 4n^{2} + 1n$ = 2n (2n + 1)2n is even 2n+1 is odd even × odd = even $\therefore (2n+1)^{2} - (2n+1) \text{ is even}$ 2. *c* is a positive integer. Prove that $\frac{6c^{3} + 30c}{3c^{2} + 15}$ is an even number. $\frac{6c (c^{2} + 5)}{3 (c^{2} + 5)} = \frac{6c}{3} = 2c$ 2c will always be even, therefore $\frac{6c^{3} + 30c}{3c^{2} + 15}$ is always even. [3]

3. a) Prove that the sum of four consecutive whole numbers is always even.

$$n+n+1+n+2+n+3 = 4n + 6$$

= 2(2n+3)
a multiple of 2, therefore even. [3]

b) Give an example to show that the sum of four consecutive integers is not always divisible by 4.

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[2]



4. Here are the first five terms of an arithmetic sequence.

Prove that the difference between the squares of any two terms of the sequence is always a multiple of 24

nth term of sequence 1s
$$6n+1$$
.
Next term can be expressed as $6n+7$
 $(6n+7)^2 - (6n+1)^2$
 $= 36n^2 + 89n + 49 - 36n^2 - 12n - 1$
 $= 72n + 48$
 $= 24(3n+2)$
which is a multiple of 24.

[6]

5. The product of two consecutive positive integers is added to the larger of the two integers.

Prove that the result is always a square number.

$$n(n+1) + n+1 = n^{2}+n+n+1$$

= n²+2n+1
= (n+1)²
which is the square of the larger number. [3]

6. Prove algebraically that the difference between the squares of any two consecutive integers is equal to the sum of these two integers.

$$(n+1)^{2} - n^{2} = n^{2} + 2n + 1 - n^{2}$$

= 2n + 1
= n + n + 1
which is the sum of the two [4]
integers.

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CREDITS AND NOTES

Question	Awarding Body
1	Pearson Edexcel
2	AQA
3	OCR
4	Pearson Edexcel
5	Pearson Edexcel
6	Pearson Edexcel

Notes:

These questions have been retyped from the original sample/specimen assessment materials and whilst every effort has been made to ensure there are no errors, any that do appear are mine and not the exam board s (similarly any errors I have corrected from the originals are also my corrections and not theirs!).

Please also note that the layout in terms of fonts, answer lines and space given to each question does not reflect the actual papers to save space.

These questions have been collated by me as the basis for a GCSE working party set up by the GLOW maths hub - if you want to get involved please get in touch. The objective is to provide support to fellow teachers and to give you a flavour of how different topics "could" be examined. They should not be used to form a decision as to which board to use. There is no guarantee that a topic will or won't appear in the "live" papers from a specific exam board or that examination of a topic will be as shown in these questions.



Links:

AQA http://www.aqa.org.uk/subjects/mathematics/gcse/mathematics-8300

OCR http://ocr.org.uk/gcsemaths

Pearson Edexcel http://qualifications.pearson.com/en/qualifications/edexcel-gcses/mathematics-2015.html

WJEC Eduqas http://www.eduqas.co.uk/qualifications/mathematics/gcse/

Contents:

This version contains questions from:

AQA – Sample Assessment Material, Practice set 1 and Practice set 2

OCR – Sample Assessment Material and Practice set 1

Pearson Edexcel – Sample Assessment Material, Specimen set 1 and Specimen set 2

WJEC Eduqas - Sample Assessment Material