Algebra - Notation, vocabulary and manipulation

| KS3 Alg (a) | Use and interpret algebraic notation, including: <br> - $a b$ in place of $a \times b$ <br> - $3 y$ in place of $y+y+y$ and $3 x y$ <br> - $a^{2}$ in place of $a \times a, a^{3}$ in place of $a \times a \times a, a^{2} b$ in place of $a \times a \times b$ <br> - $a / b$ in place of $a \div b$ <br> - coefficients written as fractions rather than as decimals <br> - brackets |
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| KS4 Alg (1) | Use and interpret algebraic notation, including: <br> - $a b$ in place of $a \times b$ <br> - $3 y$ in place of $y+y+y$ and $3 x y$ <br> - $a^{2}$ in place of $a \times a, a^{3}$ in place of $a \times a \times a, a^{2} b$ in place of $a \times a \times b$ <br> - $a / b$ in place of $a \div b$ <br> - coefficients written as fractions rather than as decimals <br> - brackets |
| KS3 Alg (b) | Substitute numerical values into formulae and expressions, including scientific formulae |
| KS4 Alg (2) | Substitute numerical values into formulae and expressions, including scientific formulae |
| KS3 Alg (c) | Understand and use the concepts and vocabulary of expressions, equations, inequalities, terms and factors |
| KS4 Alg (3) | Understand and use the concepts and vocabulary of expressions, equations, formulae, identities inequalities, terms and factors |
| KS3 Alg (d) | Simplify and manipulate algebraic expressions to maintain equivalence by: <br> - Collecting like terms <br> - Multiplying a single term over a bracket <br> - taking out common factors <br> - expanding products of two or more binomials |
| KS4 Alg (4) | Simplify and manipulate algebraic expressions (including those involving surds and algebraic fractions) by: <br> - collecting like terms <br> - multiplying a single term over a bracket <br> - taking out common factors <br> - expanding products of two or more binomials <br> - factorising quadratic expressions of the form $x^{2}+b x+c$, including the difference of two squares; factorising quadratic expressions of the form $a x^{2+} b x+c$ <br> - simplifying expressions involving sums, products and powers, including the laws of indices |
| KS3 Alg (e) | Understand and use standard mathematical formulae; rearrange formulae to change the subject |
| KS4 Alg (5) | Understand and use standard mathematical formulae; rearrange formulae to change the subject |
| KS4 Alg (6) | Know the difference between an equation and an identity; argue mathematically to show algebraic expressions are equivalent, and use algebra to support and construct arguments and proofs |
| KS4 Alg (7) | Where appropriate, interpret simple expressions as functions with inputs and outputs; interpret the reverse process as the 'inverse function'; interpret the succession of two functions as a 'composite function'. |
| Algebra - Gr |  |
| KS3 Alg (h) | Work with coordinates in all four quadrants |
| KS4 Alg (8) | Work with coordinates in all four quadrants |
| KS3 Alg (i) | Recognise, sketch and produce graphs of linear and quadratic functions of one variable with appropriate scaling, using equations in $x$ and $y$ and the Cartesian plane |
| KS3 Alg (k) | Reduce a given linear equation in two variables to the standard form $y=m x+c$; calculate and interpret gradients and intercepts of graphs of such linear equations numerically, graphically and algebraically |
| KS4 Alg (9) | Plot graphs of equations that correspond to straight-line graphs in the coordinate plane; use the form $y=m x+c$ to identify parallel and perpendicular lines; find the equation of the line through two given points, or through one point with a given gradient |
| KS4 Alg (10) | Identify and interpret gradients and intercepts of linear functions graphically and algebraically |
| KS4 Alg (11) | Identify and interpret roots, intercepts, turning points of quadratic functions graphically; deduce roots algebraically and turning points by completing the square |
| KS4 Alg (12) | Recognise, sketch and interpret graphs of linear functions, quadratic functions, simple cubic functions, the reciprocal function $y=1 / x$ with $x \neq 0$, exponential functions $=x y k$ for positive values of $k$, and the trigonometric functions (with arguments in degrees) $y=\sin x, y=\cos x$ and $y=\tan x$ for angles of any size |
| KS4 Alg (13) | Sketch translations and reflections of a given function |
| KS4 Alg (14) | Plot and interpret graphs (including reciprocal graphs and exponential graphs) and graphs of non-standard functions in real contexts, to find approximate solutions to problems such as simple kinematic problems involving distance, speed and acceleration |
| KS4 Alg (15) | Calculate or estimate gradients of graphs and areas under graphs (including quadratic and other nonlinear graphs), and interpret results in cases such as distance-time graphs, velocity-time graphs and graphs in financial contexts |
| KS4 Alg (16) | Recognise and use the equation of a circle with centre at the origin; find the equation of a tangent to a circle at a given point. |

Algebra - Solving equations and inequalities

| KS3 Alg (f) | Model situations or procedures by translating them into algebraic expressions or formulae and by using graphs |
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| KS3 Alg (j) | Interpret mathematical relationships both algebraically and graphically |
| KS3 Alg (1) | Use linear and quadratic graphs to estimate values of $y$ for given values of $x$ and vice versa and to find approximate solutions of simultaneous linear equations |
| KS3 Alg (m) | Find approximate solutions to contextual problems from given graphs of a variety of functions, including piece-wise linear, exponential and reciprocal graphs |
| KS3 Alg (g) | Use algebraic methods to solve linear equations in one variable (including all forms that require rearrangement) |
| KS4 Alg (17) | Solve linear equations in one unknown algebraically (including those with the unknown on both sides of the equation); find approximate solutions using a graph |
| KS4 Alg (18) | Solve quadratic equations (including those that require rearrangement) algebraically by factorising, by completing the square and by using the quadratic formula; find approximate solutions using a graph |
| KS4 Alg (19) | Solve two simultaneous equations in two variables (linear/linear or linear/quadratic) algebraically; find approximate solutions using a graph |
| KS4 Alg (20) | Find approximate solutions to equations numerically using iteration |
| KS4 Alg (21) | Translate simple situations or procedures into algebraic expressions or formulae; derive an equation (or two simultaneous equations), solve the equation(s) and interpret the solution. |
| KS4 Alg (22) | Solve linear inequalities in one or two variable(s), and quadratic inequalities in one variable; represent the solution set on a number line, using set notation and on a graph |
| Algebra - Sequences |  |
| KS3 Alg ( n ) | Generate terms of a sequence from either a term-to-term or a position-to-term rule |
| KS4 Alg (23) | Generate terms of a sequence from either a term-to-term or a position-to-term rule |
| KS3 Alg (0) | Recognise arithmetic sequences and find the nth term |
| KS3 Alg (p) | Recognise geometric sequences and appreciate other sequences that arise. |
| KS4 Alg (24) | Recognise and use sequences of triangular, square and cube numbers, simple arithmetic progressions, Fibonacci type sequences, quadratic sequences, and simple geometric progressions ( $r^{n}$ where $n$ is an integer, and $r$ is a rational number $>0$ or a surd) and other sequences |
| KS4 Alg (25) | Deduce expressions to calculate the $\mathrm{n}^{\text {th }}$ term of linear and quadratic sequences. |

