## Substitution, Solving \& Rearranging Equations (F)

A collection of 9-1 Maths GCSE Sample and Specimen questions from AQA, OCR, Pearson-Edexcel and WJEC Eduqas.

| Name: |  |
| :---: | :--- |
| Total Marks: |  |

1. Solve.
$3 x^{2}=75$

$$
\begin{equation*}
x= \tag{2}
\end{equation*}
$$

2. Solve.

$$
3 x+7=19
$$

$$
\begin{equation*}
x= \tag{2}
\end{equation*}
$$

3. Here is a formula.
$T=5 r+3 u$
Work out the value of $T$ when $r=8$ and $u=9$.
4. Six equations are shown below, each labelled with a letter.

| A |
| :---: |
| $y=-6 x$ |



| D |
| :---: |
| $x=\frac{6}{y}$ |


| E |
| :---: |
| $y=6 x$ |


| F |
| :---: |
| $y=\frac{2}{x}+2$ |

Choose the correct letters to make this statement true.
Equation $B$ and equation $\qquad$ are equivalent.
5. Solve.

$$
5 x=2 x+18
$$

$$
\begin{equation*}
x= \tag{2}
\end{equation*}
$$

6. (a) Solve.
(i) $2 x=18$
(a)(i) $x=$
(ii) $x+2=5$
(ii) $x=$
(iii) $\frac{x}{3}=15$

$$
\begin{equation*}
\text { (iii) } x= \tag{1}
\end{equation*}
$$

(b) (i) Find the value of t when $\mathrm{g}=4$ and $\mathrm{h}=7$.

$$
\mathrm{t}=12 \mathrm{~g}-5 \mathrm{~h}
$$

$$
\begin{equation*}
\text { (b)(i) } t= \tag{2}
\end{equation*}
$$

(ii) Rearrange to make $r$ the subject.

$$
4 r-p=q
$$

(ii)
7. Show that $3 r=2\left(5 \mathrm{k}^{2}-2 r\right)$ can be rearranged to $\mathrm{k}=\sqrt{\frac{7 r}{10}}$
8. Find the value of $a-b$ when $a=3$ and $b=-2$.
9. Solve.

$$
3 a+10=a+40
$$

$$
\begin{equation*}
a= \tag{3}
\end{equation*}
$$

10. Here are three expressions.
$\frac{b}{a}$
$b-a$
$a b$

When $\mathrm{a}=2$ and $\mathrm{b}=-6$ which expression has the smallest value?
You must show your working.
11. Kelly is trying to work out the two values of $w$ for which $3 w-w^{3}=2$

Her values are 1 and -1
Are her values correct?
You must show your working.
12. Solve $4 x+5=x+26$

$$
x=
$$

$\qquad$
13. Solve $3 x-5=9$
$\qquad$
14. $f=5 x+2 y$
$x=3$ and $y=-2$
Find the value of $f$.
15. $q=\frac{p}{r}+s$

Make $p$ the subject of this formula.
16. Here is a number machine.

(a) Work out the output when the input is 4
(b) Work out the input when the output is 11
(c) Show that there is a value of the input for which the input and the output have the same value.
17. Solve $3 x+7=1$

$$
\begin{equation*}
x= \tag{2}
\end{equation*}
$$

18. $f=6, \quad g=5$
Work out the value of $3 f-2 g$
19. Solve $5 p=3 p+8$
20. Make $t$ the subject of the formula $y=\frac{t}{3}-2 a$
21. (a) Alan is looking at number machine problems.


He says,
"If I know y I can work out x. I subtract 3 then I add 5."
Does this method work?
Give a reason for your answer.
(b)


He says,
"If I know d I can work out c. I divide by 3, then subtract 5."
Does this method work?
Give a reason for your answer.
22. Solve $5 w-11=24$
23. A company has bikes for hire.

The cost, $£ C$, to hire a bike for n days is given by the formula

$$
C=12+\frac{27}{4}(n-1)
$$

(a) Write down the cost to hire a bike for 1 day.
(b)

## Special offer

Hire a bike for $£ 9$ per day

Is it cheaper to hire a bike for 7 days using the special offer?
You must show your working.
(c) The graph shows the cost to hire a bike for one to five days at a different company.


The cost, $£ C$, to hire a bike for $n$ days using this company is given by the formula

$$
C=a+b(n-1)
$$

Work out the values of $a$ and $b$.

$$
\begin{equation*}
a= \tag{3}
\end{equation*}
$$

$\qquad$ $b=$ $\qquad$
24. Here are two number machines, $A$ and $B$.


Both machines have the same input.
Work out the input that makes the output of A three times the output of B.
25. Solve $4(x+5)=15$
26. Work out the value of $5 x+9 y$ when $x=7$ and $y=-2$
27. Solve $4 x-5=17$
28. Here is a formula.

$$
V=\frac{1}{2} x^{2} h
$$

Work out the value of $V$ when $x=11$ and $h=6$
29. Solve $12 x=3$

Circle your answer.

$$
x=-9 \quad x=\frac{1}{4} \quad x=4 \quad x=36
$$

30. You are given that $a=3$ and $b=5$

Tick whether each statement is true or false.
Give a reason for each answer.

| Statement | True | False | Reason |
| :---: | :--- | :--- | :--- |
| $a b=35$ |  |  |  |
| $2 b^{2}=100$ |  |  |  |
|  |  |  |  |

31. (a) Solve $4 x=16$
(b) Solve $\frac{y}{5}=4$
(c) Solve $5 a-8=17$
32. Using the formula below, find the value of k when $\mathrm{p}=50$ and $\mathrm{q}=10$.

You must show all your working.

$$
2 q=p-10 k
$$

33. (a) Solve $4 c+5=11$

$$
\begin{equation*}
c= \tag{2}
\end{equation*}
$$

(b) Solve $5(e+7)=20$

$$
\begin{equation*}
e= \tag{2}
\end{equation*}
$$

34. Make $t$ the subject of the formula $w=3 t+11$
35. (a) Solve $f+2 f+f=20$
$\qquad$
$f=$
(b) Solve $18-m=6$

$$
\begin{equation*}
m= \tag{1}
\end{equation*}
$$

36. Complete this table of values.

37. Solve $x-7=56$

Circle your answer.

$$
x=8 \quad x=49 \quad x=56 \quad x=63
$$

38. Here is a number machine.

a) Work out the output when the input is 12
b) Work out the input when the output is 27
c) Write $y$ as an expression in terms of $x$.
39. Work out the value of $4(2 x+3 y)$ when $x=8$ and $y=-3$
40. This formula works out the tax you pay.

$$
T=0.2(E-10600)
$$

$T$ is the tax you pay in pounds.
$E$ is the amount you earn in pounds.
a) How much tax do you pay if you earn $£ 20000$ ?
b) What is the most you can earn without paying tax?
c) Alison pays $£ 5200$ tax.

Work out the amount she earns.
41. Solve $x^{2}=30.25$
42. Solve $\frac{2 x}{5}+1=13$
43. The area of an ellipse, width $a$ and height $b$, is given by


A rectangular photograph measures 15 cm by 10 cm
It is put into a frame as shown.


The part of the photograph that can be seen is an ellipse.
Work out the percentage of the photograph that can be seen.

## CREDITS AND NOTES

| Q | Awarding Body | $\mathbf{Q}$ | Awarding Body | Q | Awarding Body | $\mathbf{Q}$ | Awarding Body |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | OCR | 15 | Pearson Edexcel | 29 | AQA | 43 | AQA |
| 2 | OCR | 16 | Pearson Edexcel | 30 | AQA |  |  |
| 3 | OCR | 17 | Pearson Edexcel | 31 | WJEC Eduqas |  |  |
| 4 | OCR | 18 | Pearson Edexcel | 32 | WJEC Eduqas |  |  |
| 5 | OCR | 19 | Pearson Edexcel | 33 | Pearson Edexcel |  |  |
| 6 | OCR | 20 | Pearson Edexcel | 34 | Pearson Edexcel |  |  |
| 7 | OCR | 21 | AQA | 35 | Pearson Edexcel |  |  |
| 8 | OCR | 22 | AQA | 36 | Pearson Edexcel |  |  |
| 9 | OCR | 23 | AQA | 37 | AQA |  |  |
| 10 | AQA | 24 | AQA | 38 | AQA |  |  |
| 11 | AQA | 25 | AQA | 39 | AQA |  |  |
| 12 | Pearson Edexcel | 26 | AQA | 40 | AQA |  |  |
| 13 | Pearson Edexcel | 27 | AQA | 41 | AQA |  |  |
| 14 | Pearson Edexcel | 28 | AQA | 42 | AQA |  |  |

## Notes:

These questions have been retyped from the original sample/specimen assessment materials and whilst every effort has been made to ensure there are no errors, any that do appear are mine and not the exam board s (similarly any errors I have corrected from the originals are also my corrections and not theirs!).

Please also note that the layout in terms of fonts, answer lines and space given to each question does not reflect the actual papers to save space.

These questions have been collated by me as the basis for a GCSE working party set up by the GLOW maths hub - if you want to get involved please get in touch. The objective is to provide support to fellow teachers and to give you a flavour of how different topics "could" be examined. They should not be used to form a decision as to which board to use. There is no guarantee that a topic
 will or won't appear in the "live" papers from a specific exam board or that examination of a topic will be as shown in these questions.

## Links:

AQA http://www.aqa.org.uk/subjects/mathematics/gcse/mathematics-8300
OCR http://ocr.org.uk/gcsemaths
Pearson Edexcel http://qualifications.pearson.com/en/qualifications/edexcel-gcses/mathematics-2015.html
WJEC Eduqas http://www.eduqas.co.uk/qualifications/mathematics/gcse/

## Contents:

This version contains questions from:
AQA - Sample Assessment Material, Practice set 1 and Practice set 2
OCR - Sample Assessment Material and Practice set 1
Pearson Edexcel - Sample Assessment Material, Specimen set 1 and Specimen set 2
WJEC Eduqas - Sample Assessment Material

